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## Novel recruitment method

Some time ago Google advertised for employees by using the following message on a roadside billboard: 'first 10-digit prime found in consecutive digits of e].com'

That is, potential employees had to locate the first occurrence of a 10-digit prime number in consecutive digits of the mathematical constant  $e$ . This number gave the web address of a more difficult mathematical question.

How do we find this 10-digit prime number? *Mathematica* has the necessary functions to make this relatively easy.

The function `RealDigits[x, b, len]` gives  $len$  digits of the number  $x$  in base  $b$ . Hence the first 10 digits of  $e$  in base 10 is obtained from:

```
In[2]:= RealDigits[e, 10, 10]
Out[2]= {{2, 7, 1, 8, 2, 8, 1, 8, 2, 8}, 1}
```

The 10 digits are shown together with the number of digits in the integer part (1). We can then form the 10-digit number by first extracting the list of digits

```
In[3]:= RealDigits[e, 10, 10][[1]]
Out[3]= {2, 7, 1, 8, 2, 8, 1, 8, 2, 8}
```

followed by applying the function `FromDigits`:

```
In[4]:= FromDigits[RealDigits[e, 10, 10][[1]]]
Out[4]= 2718281828
```

which we can test for primality using `PrimeQ`:

```
In[5]:= PrimeQ[FromDigits[RealDigits[e, 10, 10][[1]]]]
Out[5]= False
```

Now we need to be able to extract 10 consecutive digits commencing at an arbitrary position.

We do this using `RealDigits[x, b, len, n]` which gives  $len$  digits starting with the coefficient of  $b^n$ .

We create a function with argument  $j$  to start the 10 digits at position  $10^j$ :

```
edigits[j_]:=RealDigits[e,10,10,-j]
```

We can use a `For` statement to repeat the process until we locate the first 10-digit prime.

The counter  $i$  is set initially to 0 and incremented by 1 provided the 10-digit number is not prime; the process stops when a prime number is found.

```
In[6]:= For[i = 0, PrimeQ[FromDigits[RealDigits[e, 10, 10, -i][[1]]]] == False, i++];
```

We use this incremented value of  $i$  to give the 10-digit prime:

```
In[7]:= FromDigits[RealDigits[e, 10, 10, -i][[1]]]
Out[7]= 7427466391
```

Thus 7427466391 is the first 10-digit prime from consecutive digits of  $e$ .

Here are the first 120 digits of  $e$  with the 10-digit prime in red:

$N[e, 120]$

2.71828182845904523536028747135266249775  
7247093699959574966967627724076630353547  
5945713821785251664274274663919320030599